

$$\text{Cor}\left(\bigoplus_{i=1}^n V_{il}, P\right) \leq 2^{-\Omega(n)}$$